### Solid-State Chemistry

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# Crystal Structures of and Displacive Transitions in OsN<sub>2</sub>, IrN<sub>2</sub>, RuN<sub>2</sub>, and RhN2\*\*

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Solid nitrides are attracting increasing interest due to their importance in both fundamental science and technological applications.<sup>[1-5]</sup> Recently, the nitrides of Os, Ir, and Pt were synthesized under extreme conditions. [6-14] These discoveries are quite surprising since the noble transition metals (Os, Ir, Pt, Ru, Rh, Pd) were for many years thought not to form nitrides.[15,16] This emerging field has attracted much interest. [6-14,17] and these compounds have been shown to have very intriguing properties, such as an ultra-high bulk modulus (428 GPa for IrN<sub>2</sub>).<sup>[11]</sup> To date, however, only the crystal structure of PtN<sub>2</sub> has been solved; [10,12-14] the crystal structures of IrN2 and OsN2 are still an open question. Because the crystal structure is an important prerequisite for understanding the properties of crystalline solids,[18] the lack of such information has hindered the development of this new field.

We show herein by density functional calculations that IrN<sub>2</sub> and OsN<sub>2</sub> crystallize in structural types that have never been observed in nitrides. On the basis of this finding, we predict the crystal structures of RuN<sub>2</sub> and RhN<sub>2</sub>, which have not yet been synthesized. We also predict that IrN2 should display an especially interesting behavior among these nitrides: at ambient pressure it is predicted to adopt a lowsymmetry structure that is semiconducting owing to a Peierls distortion, but high pressures are predicted to induce a semiconductor-metal transition and a second-order displacive phase transition. All of these phases have a common structural feature, namely quasimolecular N<sub>2</sub> units.

A variety of structure types were considered when searching for the crystal structures of IrN2, OsN2, RuN2, and RhN<sub>2</sub>, including the pyrite (cubic), fluorite (cubic), rutile (tetragonal), marcasite (orthorhombic, also called the CaCl<sub>2</sub> type, Figure 1 left), and CoSb<sub>2</sub> (monoclinic, Figure 1 right) types.[19] Except for the fluorite-type structures, all of these

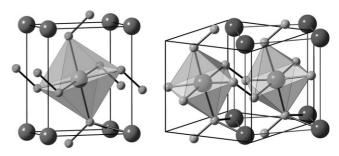


Figure 1. Unit cells of the marcasite (left) and CoSb<sub>2</sub> (right) structure types. The large and small spheres represent the metal cations and the anions, respectively. The CoSb<sub>2</sub> structure can be viewed as a distortion of the marcasite structure with a doubled unit cell.

phases are composed of MN<sub>6</sub> polyhedra (M = noble metal) that share corners in the pyrite-type structure and edges in the other structures. The marcasite-type structure can be viewed

as a distorted rutile-type structure with the N-N bonds

formed by a small distortion and rotation of the MN<sub>6</sub>

polyhedra. SiO<sub>2</sub> is the most extensively studied compound

with a displacive phase transition between the rutile and the marcasite structure types.[20] Further distortion from the

marcasite structure type results in the CoSb<sub>2</sub> structure type.

differences. First-principles calculations allow an accurate

evaluation of the total energy of a system as a function of the

atomic positions and stress, and are therefore a powerful tool

in high-pressure research.<sup>[1,21]</sup> The total energies of IrN<sub>2</sub>,

difference is 0.15 eV per formula unit for IrN<sub>2</sub> at 0 GPa. More

details, including the transition pressure, are given below. For

The competing structures generally have small energy

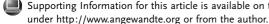
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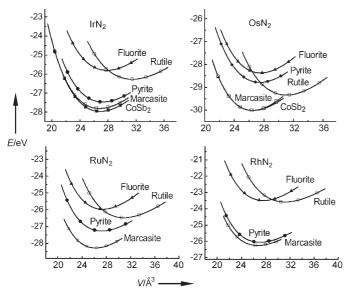
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OsN<sub>2</sub>, RuN<sub>2</sub>, and RhN<sub>2</sub> as a function of the volume for various structure types are given in Figure 2. As can be seen, for IrN<sub>2</sub> and OsN<sub>2</sub>, the CoSb<sub>2</sub> structure type has the lowest energy at low pressures; the structural parameters of CoSb<sub>2</sub>-type IrN<sub>2</sub> and OsN<sub>2</sub> are given in Table 1. It is interesting to note that the energy differences between the CoSb<sub>2</sub> and the marcasite structure types for both IrN2 and OsN2 decrease continuously to zero with decreasing volume, thereby suggesting a pressure-induced continuous structural transition. The energy







**Figure 2.** Energy–volume relationships (per formula unit) for  $IrN_2$ ,  $OsN_2$ ,  $RuN_2$ , and  $RhN_2$  in different structure types over the pressure range -30–200 GPa.

**Table 1:** Lattice parameters (a, b, c; in Å) and atomic positions (x, y, z) for IrN<sub>2</sub>, OsN<sub>2</sub>, RuN<sub>2</sub>, and RhN<sub>2</sub>.

Compound (pressure)		a or x	b or y	c or z
CoSb <sub>2</sub> -type <sup>[a]</sup>				
IrN <sub>2</sub> (0 GPa)	lattice	4.809	4.858	4.848
- 、	lr	0.234	0.000	0.221
	N1	0.186	0.598	0.299
	N2	0.325	0.413	0.159
$OsN_2$ ( $-5$ GPa)	lattice	4.886	4.873	4.913
	Os	0.235	0.000	0.225
	N1	0.192	0.596	0.307
	N2	0.321	0.406	0.176
Marcasite-type <sup>[b]</sup>				
IrN <sub>2</sub> (170 GPa)	lattice	3.805	4.508	2.434
- ,	N	0.127	0.403	0
OsN <sub>2</sub> (43 GPa)	lattice	4.004	4.753	2.553
- ,	N	0.126	0.403	0
OsN <sub>2</sub> (0 GPa)	lattice	4.092	4.878	2.653
	N	0.127	0.404	0
RuN <sub>2</sub> (0 GPa)	lattice	4.058	4.847	2.665
• •	N	0.123	0.408	0
RhN <sub>2</sub> (0 GPa)	lattice	4.010	4.827	2.758
	N	0.124	0.413	0

[a] The low-pressure polymorphs of IrN $_2$  and OsN $_2$  adopt the CoSb $_2$  structure type in space group  $P2_1/c$ . The 12 atoms in the unit cell occupy three sets of the 4e Wyckoff position (x, y, z). For IrN $_2$  (0 GPa),  $\beta$  = 108.25° and for OsN $_2$  (–5 GPa),  $\beta$  = 112.94°. [b] RuN $_2$ , RhN $_2$ , and the high-pressure polymorphs of IrN $_2$  and OsN $_2$  adopt the marcasite structure type in space group Pnnm. There are six atoms in the unit cell: the two metal atoms occupy the 2a Wyckoff position (0, 0, 0), and the four nitrogen atoms the 4g Wyckoff position (x, y, 0).

 $RuN_2$  and  $RhN_2$ , the  $CoSb_2$ -type structure relaxes to the marcasite-type structure at all pressures.

Recently, Crowhurst et al. [10] reported the synthesis of IrN<sub>2</sub> and its Raman spectra at both ambient and high

pressures. The low symmetry of IrN2 was inferred from the complexity of the Raman spectra. Young et al.[11] reported the synthesis of OsN2 and IrN2 and the corresponding X-ray diffraction data. OsN<sub>2</sub> was indexed as orthorhombic.<sup>[11]</sup> Although the atomic positions were not given, the cell dimensions match the present results for the marcasite-type structure well (within 3%). IrN<sub>2</sub> was indexed as hexagonal, with several low-intensity peaks unassigned. The X-ray diffraction patterns of OsN<sub>2</sub> and IrN<sub>2</sub> at 43 and 64 GPa, respectively, were also given. Therefore, in order to make a direct comparison, we calculated the structural parameters of IrN<sub>2</sub> and OsN<sub>2</sub> at these high pressures. The corresponding Xray diffraction patterns (Figure S1) match excellently with the experimental ones (including the weak peaks not assigned to the hexagonal unit cell for IrN2) and thus support the marcasite structure for OsN2 and the CoSb2 structure for IrN<sub>2</sub> at those pressures.

The weak X-ray scattering of nitrogen relative to the noble transition metals makes it difficult to determine the crystal structures of the compounds from the X-ray data of the tiny high-pressure samples conclusively. [10,12,13] Raman spectroscopy, which does not have this drawback, played an important role in the determination of the crystal structure of PtN<sub>2</sub>. Therefore, the Raman-active phonon frequencies of the compounds investigated herein were calculated and compared to the existing experimental results. To the best of our knowledge, a symmetry analysis of the phonon modes has not been reported previously for any CoSb<sub>2</sub>-type compound. From group-theory analysis, the irreducible representations of the zone-center optical phonon modes of the CoSb<sub>2</sub> structure are  $\Gamma^{opt} = 9 A_g + 9 B_g + 8 A_u + 7 B_u$ , where the  $A_g$ and  $B_{\mbox{\tiny g}}$  modes are Raman-active while the  $A_{\mbox{\tiny u}}$  and  $B_{\mbox{\tiny u}}$  modes are infrared-active. The Raman-active phonon modes of IrN<sub>2</sub>, as listed in Table 2, were assigned by analyzing the symmetry of each eigenmode. The calculated Raman frequencies match very well (within 4%, see Figure S2) with the experimental values at both ambient and high pressures,[10] thereby confirming the CoSb<sub>2</sub> structure for IrN<sub>2</sub>.

Table 2: Frequencies (in cm<sup>-1</sup>) of the Raman modes of CoSb<sub>2</sub>-type IrN<sub>2</sub>.

Compound (pressure)	B <sub>g</sub>	Ag	B <sub>g</sub>	Ag	Bg	A <sub>g</sub>
IrN <sub>2</sub> (0 GPa)	193	197	215	216	274	275
, ,	590	592	596	604	641	645
	669	666	856	830	911	868
IrN <sub>2</sub> (48 GPa)	210	215	230	231	315	316
-	665	670	672	675	724	725
	772	772	965	949	1069	1026

The marcasite structure has six Raman modes, one  $B_{2g}$ , one  $B_{3g}$ , two  $A_g$ , and two  $B_{1g}$  modes. The frequencies for marcasite-type  $OsN_2$ ,  $RuN_2$ , and  $RhN_2$  are given in Table 3. The Raman spectra for  $OsN_2$  could not be observed experimentally. On the basis of this fact and the fact that at Raman scattering signals from metals are very weak owing to the low penetration depth of the laser in metals, Young et al. inferred that  $OsN_2$  has a metallic nature; this hypothesis was corroborated by the electronic-structure analysis given below.

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**Table 3:** Frequencies (in cm<sup>-1</sup>) of the Raman modes of marcasite-type OsN<sub>2</sub>, RuN<sub>2</sub>, and RhN<sub>2</sub>.

Compound (pressure)	$B_{3g}$	$B_{2g}$	$A_g$	$B_{1g}$	$A_g$	B <sub>1g</sub>
OsN <sub>2</sub> (0 GPa)	538	561	797	811	850	890
OsN <sub>2</sub> (50 GPa)	594	618	909	915	1011	1051
RuN <sub>2</sub> (0 GPa)	522	542	691	725	1027	1043
RuN <sub>2</sub> (50 GPa)	584	606	813	851	1158	1184
RhN <sub>2</sub> (0 GPa)	511	471	712	728	1140	1150
RhN <sub>2</sub> (50 GPa)	592	557	848	874	1252	1268

The bulk moduli (B) of the compounds and their pressure derivatives (B') were calculated by fitting the energy-volume curves to the Birch–Murnaghan equation-of-state. The bulk moduli of OsN<sub>2</sub>, IrN<sub>2</sub>, RuN<sub>2</sub>, and RhN<sub>2</sub> are 374 (B'=5.49), 402 (4.32), 343 (5.11), and 286 GPa (5.58), respectively. These values match the experimental results (358 GPa for OsN<sub>2</sub> and 428 GPa for IrN<sub>2</sub>)<sup>[11]</sup> within about 5%, which is typical for local density approximation (LDA) calculations. For comparison, the bulk modulus of PtN<sub>2</sub> is about 354 GPa. <sup>[6,10,12]</sup> IrN<sub>2</sub>, which has the highest bulk modulus, is the least compressible of the compounds.

All the noble-metal nitrides (or pernitrides, as suggested earlier, [14] to highlight the quasimolecular nature of the N<sub>2</sub> units) are composed of MN<sub>6</sub> octahedra connected by N-N bonds. The N-N bond lengths of the 5d noble-metal pernitrides are nearly the same (1.40 (OsN<sub>2</sub>), 1.42 (IrN<sub>2</sub>), 1.42 Å (PtN<sub>2</sub>)), and the N-N bonds of the 4d noble-metal pernitrides are a little shorter (1.34 Å (RuN<sub>2</sub>), 1.30 Å (RhN<sub>2</sub>)), suggesting the presence of more "free" N<sub>2</sub> quasimolecules. This result is possibly due to the weaker bonding interaction between N<sub>2</sub> and the metal atoms, as manifested by the lower bulk moduli of RuN2 and RhN2. Previous studies have shown that an important stabilizing effect in PtN<sub>2</sub> comes from strong covalent N-N bonding, which is comparable to the C-C bonding in diamond and the single bonds in the polymeric phase of nitrogen.<sup>[10-13,22]</sup> By reinforcing the network formed by the MN<sub>6</sub> octahedra, this strong covalent N-N bonding also provides a strengthening effect in the compounds, which results in their high elastic moduli. This suggests a pathway to form strong solids by employing strong N-N bonds instead of breaking them, as occurs in most nitrides.

We will now describe an interesting structural distortion and a pressure-induced semiconductor-metal transition in the compounds. The electronic structure is also given to show its correlation with the structural stability. The electronic density of states (DOS) curve of  $OsN_2$  is shown in Figure 3 a. There is no energy gap, which indicates that  $OsN_2$  is indeed metallic and supports the previous inference based on its low Raman activity. [11] Note that the Fermi level lies close to a minimum in the DOS, which is a typical indication of structural stability.

The DOS curves of IrN<sub>2</sub> at zero pressure are given in Figures 3b and 3c for the (hypothetical) marcasite structure and the ground-state CoSb<sub>2</sub> structure, respectively. With one more valence electron than OsN<sub>2</sub>, IrN<sub>2</sub> in the marcasite structure has its Fermi level shifted away from the local DOS minimum, which implies that IrN<sub>2</sub> is less stable in the marcasite structure. However, an energy gap at the Fermi

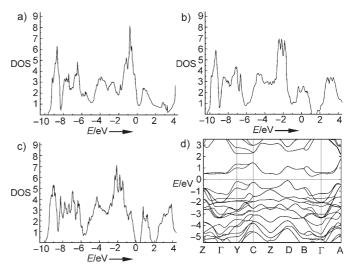


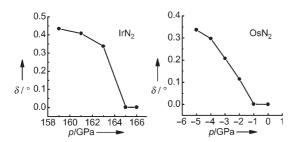
Figure 3. DOS curves for a) OsN<sub>2</sub> and b) IrN<sub>2</sub> in the marcasite structure. c) DOS curve and d) band structure of IrN<sub>2</sub> in the ground-state CoSb<sub>2</sub> structure. The Peierls distortion of IrN<sub>2</sub> results in the opening of an energy gap. The Fermi levels are located at 0 eV.

level can be opened by a small distortion to the  $CoSb_2$ -type structure. This monoclinic distortion is a typical Peierls distortion, which reduces the symmetry of a crystal and lifts the degeneracy near the Fermi energy of the undistorted structure, thereby forming an energy gap. A net energy reduction results from occupation of the states with lowered energy, while the states with raised energy are empty. The atomic mechanism of the Peierls distortion in  $IrN_2$  can be attributed to a metal–metal interaction, as described below. The band structure of  $IrN_2$  is shown in Figure 3d. The top of the valence band is located at D, and the bottom of the conduction band is located between  $\Gamma$  and B, with an indirect energy gap of 0.4 eV. The true gap should be larger, however, since LDA generally underestimates the band gap.

As noted in Figure 1, the CoSb<sub>2</sub> structure type forms from the marcasite structure type by a cell-doubling distortion. The space group of the CoSb<sub>2</sub> structure (P2<sub>1</sub>/c, no. 14) is a subgroup of that of the marcasite structure (Pnnm, no. 58). According to the space-group analysis, [24] the atomic movement involved in the transition corresponds to the irreducible representation U<sub>1</sub> at the Brillouin zone boundary point U (0.5, 0, 0.5) of the marcasite structure. The basis vectors of the marcasite structure (a, b, c) correspond to  $[10\overline{1}]/2$ , [010], and [101]/2 of the CoSb<sub>2</sub> structure, respectively. The angle  $(90.5^{\circ} \text{ at } 0 \text{ GPa}) \text{ between } [10\bar{1}] \text{ and } [101] \text{ of } \text{CoSb}_2\text{-type IrN}_2$ has only a small deviation (0.5°) from the corresponding angle (90°) in the marcasite structure. This deviation, referred to as the distortion angle hereafter, is a measure of the magnitude of the monoclinic distortion in the CoSb<sub>2</sub> structure. Accompanying the unit-cell distortion, the Ir atoms displace in the marcasite [001] direction to form alternate Ir-Ir bond lengths (2.58 and 3.09 Å at 0 GPa). This atomic pairing is similar to the pairing mechanism of one-dimensional systems upon Peierls distortion.<sup>[23]</sup>

As shown in Figure 2, there is a pressure-induced phase transition in  $IrN_2$  and  $OsN_2$ . The energy and enthalpy of the

CoSb<sub>2</sub>-type phases approach those of the marcasite-type phases asymptotically. Together with the symmetry relationship, this result suggests a second-order (or continuous) transition. As the transition pressure ( $p_c$ ) for a second-order transition is ill-defined in the energy-volume and enthalpy-pressure curves, we determined  $p_c$  from the change of the structural parameters near the transition point. The pressure dependence of the distortion angle of  $IrN_2$  is given in Figure 4. With increasing pressure, the distortion angle vanishes at the transition pressure (165 GPa). The energy gap also vanishes at high pressures, but at a lower value (130 GPa) than the structural transition. This discrepancy is possibly due to the underestimation of the band gaps from the LDA calculations.



**Figure 4.** Pressure dependence of the distortion angle ( $\delta$ ) of IrN<sub>2</sub> and OsN<sub>2</sub> in the CoSb<sub>2</sub> structure. A distortion angle of  $\delta$  = 0° corresponds to the marcasite structure.

The phase-transition pressure of OsN<sub>2</sub> is much lower than that of IrN<sub>2</sub>. In fact, the LDA calculations give a negative  $p_c$ (-1 GPa), which means that OsN<sub>2</sub> would have the marcasite structure at zero pressure. The generalized-gradient approximation (GGA) calculations give a higher  $p_c$  (15 GPa), which implies a CoSb<sub>2</sub>-type ground-state structure. From the experimental results that an orthorhombic structure is observed for  $OsN_2$  at and above zero pressure, [11] it would appear that the LDA calculations predict the transition pressure better than the GGA calculations. For the elastic properties, the LDA results also match the experimental values better. [6,12] The reason for these findings are not yet clear. Furthermore, considering that  $p_c$  (-1 GPa for LDA) is close to zero pressure, it could be postulated that a tensile stress (e.g., that formed by a substrate with slightly larger lattice parameters) might stabilize the CoSb<sub>2</sub>-type structure of OsN<sub>2</sub>.

In summary, we have solved the crystal structures of  $OsN_2$  and  $IrN_2$  and predicted those of  $RuN_2$  and  $RhN_2$ . A pressure-induced displacive phase transition and semiconductor–metal transition are predicted for  $IrN_2$ , which also has an ultra-high bulk modulus. These findings suggest the rich physics of these compounds. We anticipate that more pernitrides with interesting properties can be synthesized, including, but not limited to,  $RuN_2$  and  $RhN_2$ .

We note that the marcasite- and  $CoSb_2$ -type structures have not been observed previously in nitrides. Also, while the marcasite-type structure and the related rutile-type structure have been studied intensively for oxides such as  $SiO_2$  and  $SnO_2$ , the  $CoSb_2$ -type structure has never been considered for oxides. The structural determination and the prediction of the

pressure-induced phase transition in noble-metal pernitrides presented herein may be of use in the synthesis and highpressure study of other nitrides and oxides.

#### **Experimental Section**

We studied the crystal structures and high-pressure behavior of the noble-metal pernitrides using the projector augmented-wave method<sup>[25]</sup> within density functional theory, as implemented in the VASP code. [26,27] For the exchange and correlation functional both LDA[28] and GGA proposed by Perdew, Burke, and Ernzerhof  $(PBE)^{[29]}$  were used. The LDA results are given herein, unless stated otherwise. In light of the small energy differences between the candidate structures, the calculations were carried out to a high numerical precision. The electronic wave functions were expanded using a plane-wave basis set with a cutoff energy of 500 eV. Integrations over the Brillouin zone were performed using Monkhorst–Pack grids. The k-point sampling in the Brillouin zone and the plane-wave cutoff energy were tested to ensure that the total energies converged to 1 meV per atom. The structural relaxations were performed until the residual forces and stresses (except the applied pressure) were less than 0.005 eV Å<sup>-1</sup> and 0.1 GPa, respectively.

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